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### SIXTH SEMESTER UG (CBCSS-UG) DEGREE EXAMINATION, MARCH 2024

Mathematics

MTS 6B 14 (E01)—GRAPH THEORY

(2019 Admission onwards)

Time: Two Hours

Maximum Marks: 60

## Section A (Short Answer Type Questions)

Answer any number of questions. Each question carries 2 marks. Maximum marks 20.

- 1. Find the number of edges of  $k_{2,3}$ .
- 2. Draw the graph  $K_5-\{e\}$ .
- 3. Define degree of a vertex. Explain with example.
  - 4. Let G be a simple graph in which there is no pair of adjacent edges. What can you say about the degree of the vertices in G? Justify.
  - 5. Give an example of a self-complementary graph with five vertices.
  - 6. Let G be a simple graph with n vertices and  $\overline{G}$  be its complement. Prove that, for each vertex V in G,  $d_{G}(v) + d_{\bar{G}}(v) = n - 1$ .
  - 7. A connected graph G has 21 vertices, what is the minimum possible number of edges in G.
  - 8. Define diameter of a graph G. Which simple graphs have diameter 1?
  - 9. When can you say that the wheel graph  $W_n, n \ge 4$  is Euler? Justify.
  - 10. Define Jordan curve. Give an example.
  - 11. Define Spanning tree. State Cayleys theorem in spanning trees.
  - 12. Let G be a Hamiltonian graph. Show that G does not have a cut vertex.

# Section B (Paragraph/Problem Type Questions)

Answer any number of questions. Each question carries 5 marks. Maximum marks 30,

- 13. Prove that  $k_5$ , the complete graph on five vertices, is non-planar.
- 14. Let G be a planar graph with less than 12 vertices. Prove that G has a vertex V with  $d(v) \leq 4$ .

Turn over

- Explain Konigsberg bridge problem.
- 16. Let G be a graph in which the degree of every vertex is at least two then  $pr_{0V_{\theta}}$ contains a cycle.
- 17. Prove that a vertex V of a tree T is a cut vertex if and only if d(v) > 1.
- 18. Let G be a connected graph, then G is a tree if and only if every edge of G is a brice
- 19. Given any two vertices u and v of a graph G, prove that every u-v walk contains

## Section C (Essay Type Questions)

Answer any one questions. The question carries 10 marks.

- 20. Let G be a non-empty graph with at least two vertices. Then prove that G is bipart. only if it has no odd cycle.
- 21. Prove that if T is a tree with n vertices then it has precisely n-1 edges.

 $(1 \times 10 = 1)$