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Name.....

Reg. No.....

## FOURTH SEMESTER (CBCSS—UG) DEGREE EXAMINATION APRIL 2023

Mathematics

MTS 4C 04-MATHEMATICS-4

(2019 Admission onwards)

ime: Two Hours

Maximum: 60 Marks

## Section A

Answer any number of questions.

Each question carries 2 marks.

Cailing is 20.

- 1. Solve the initial value problem  $\frac{dy}{dx} = \frac{-x}{y}$ , y(4) = -3.
- 2. Solve  $(x^2 9) \frac{dy}{dx} + xy = 0$ .
- 3. Find the value of k so that the differential equation  $(y^3 + kxy^4 2x) dx + (3xy^2 + 20x^2y^3) dy = 0$  is exact.
- 4. Verify that the functions  $e^{-3x}$ ,  $e^{4x}$  form a fundamental set of solutions of the differential equation y'' y' 12y = 0 on  $(-\infty, \infty)$ .
- 5. The function  $y_1 e^x$  is a solution of y'' y = 0 on the interval  $(-\infty, \infty)$ , use reduction of order to find a second solution  $y_2$ .
- 6. Find the general solution of y''' 4y'' 5y' = 0.
- 7. Solve the initial value problem  $y'' + 4y' + 5y = 35e^{-4x}$ , y(0) = -3, y'(0) = 1.
- 8. Find  $\mathcal{L}(f(t))$ , where  $f(t) = \sin 2t \cos 2t$ .
- 9. Evaluate  $\mathcal{L}^{-1}\left(\frac{s}{(s-2)(s-3)(s-6)}\right)$ .

Turn over

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10 Write 
$$f(t) = \begin{cases} 2, & 0 \le t < 3 \\ -2, & t \ge 3 \end{cases}$$
 in terms of unit step functions and find  $\mathcal{L}(f(t))$ 

- 11. Show that the functions  $f_1(x) = e^x$ ,  $f_2(x) = xe^{-x} e^{-x}$  are orthogonal on [0, 2],
- 12. Show that the partial differential equation  $\frac{\partial^2 u}{\partial x^2} + 6 \frac{\partial^2 u}{\partial x \partial y} + 9 \frac{\partial^2 u}{\partial y^2}$  is parabolic.

## Section B

Answer any number of questions. Each question carries 5 marks. Ceiling is 30.

13. Solve 
$$x \frac{dy}{dx} + y = x^2 y^2$$
.

14. Solve  $\frac{dy}{dx} = (x + y + 1)^2$  by using an appropriate substitution.

15. 
$$y''' + y'' = e^x \cos x$$
.

16. Solve 
$$x^2 y'' - 3xy' + 3y = 2x^4 e^x$$
.

17. Solve 
$$y' + 6y = e^{4t}$$
,  $y(0) = 2$  using the Laplace transform.

18. Evaluate 
$$\mathcal{L}^{-1}\left(\frac{1}{\left(s^2+k^2\right)^2}\right)$$
.

19. Expand f(x) = x, -2 < x < 2 in a Fourier series.

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## Section C

Answer any one question.

The question carries 10 marks.

- 20. Solve the initial value problem  $y'' 6y' + 9y = t^2 e^{3t}$ , y(0) = 2, y'(0) = 17 using Laplace transform.
- 21. Expand  $f(x) = \begin{cases} 0, & -\pi < x < 0 \\ \pi x, & 0 \le x < \pi \end{cases}$  in a Fourier series.